## CMPE 350 - Spring 2018

## PS 12 - 07.05.18

**4.30** Let A be a Turing-recognizable language consisting of descriptions of Turing machines,  $\{\langle M_1 \rangle, M_2 \rangle, \ldots\}$ , where every  $M_i$  is a decider. Prove that some decidable language D is not decided by any decider  $M_i$  whose description appears in A. (Hint: You may find it helpful to consider an enumerator for A.)

• Given an example of a language L such that L is co-Turing recognizable but its complement is not.

• Prove that the language  $\{ < M, w, q > | M \text{ is a Turing machine which visits state } q \text{ during its execution when started with input string } w \}$  is undecidable.

• Show that the set of undecidable languages are closed under complementation.

**5.9** Let  $T = \{\langle M \rangle | M \text{ is a TM that accepts } w^R \text{ whenever it accepts } w\}$ . Show that T is undecidable.